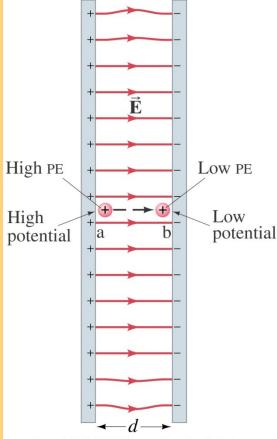
Chapter 17: Electric Potential

The electrostatic force is **conservative** – electric **potential** energy can be defined (just like for gravitational force)

Change in electric potential energy is negative of work done by electric force (independent of path):



In the figure:

$$W = Fd\cos\theta = qEd\cos\phi \Rightarrow PE_b - PE_a = -qEd$$

Angle between the electric force and the displacement

 $\phi\,$ Angle between the electric field and the displacement

Small positive charge q initially at a. Electric force does work on it and accelerates it toward b. The potential energy decreases and the particle's kinetic energy increases.

Reverse is true for negative charge.

Electric Potential

Similarly to electric field, we define **electric potential** as the potential energy per unit charge:

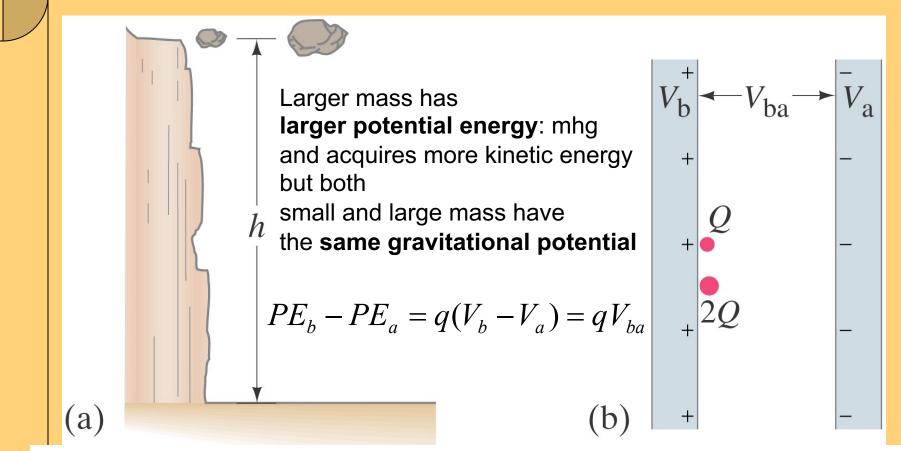
 $V_{\rm a} = \frac{12a}{q}$ Unit of electric potential: the volt (V) 1 V = 1 J/C.

Only difference in potential is meaningful, so where to choose V=0 is arbitrary

$$V_{ba} = V_{b} - V_{a} = \frac{PE_{b} - PE_{a}}{q} = -\frac{W_{ba}}{q}$$
+q has high PE in a
-q has high PE in b
-q has high PE in b
-q has high PE in b

Electric Potential vs. Potential Energy

Analogy between gravitational and electrical potential energy:

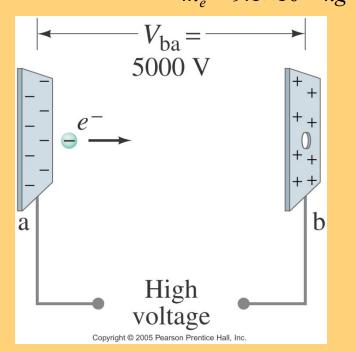


Gravitational PE depends on both m and h.g - effects of h.g depends on planet Electrical PE deps on both Q and Vab - effects of Vab deps on charges on plates

Batteries, electric generators - keep potential difference

Exercise

Ex. 17-2 Suppose an electron is accelerated from rest through a potential difference Vb – Va = Vba = +5000 V. (a) What is the change in electric potential energy of the electron? (b) What is the speed of the electron as a result of this acceleration? $m_e = 9.1 \times 10^{-31} kg$



$$\Delta PE = qV_{ba} = -8.0 \times 10^{-16} J$$
$$\Delta KE = -\Delta PE \Longrightarrow v = 4.2 \times 10^7 \, m/s$$

Proton would be accelerated from rest by a potential difference -5000 V

 $m_p = 1.67 \times 10^{-27} kg$

Electric Potential and Field

Work is charge multiplied by potentia $W = -q(V_{
m b} - V_{
m a}) = -qV_{
m ba}$

Work is also force multiplied by distance:

$$W = Fd = qEd$$

Solving for the field,	$E = -\frac{V_{\text{ba}}}{d}$
Unit: N/C or V/m	а

Signs tells us that the electric field points in the direction of **decreasing** potential V

E is VECTOR V is SCALAR

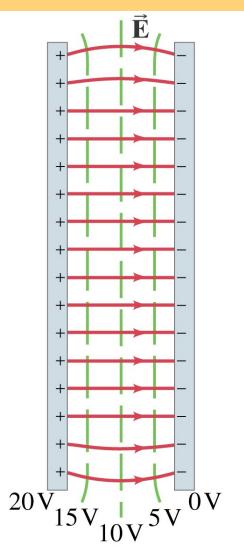
Ex. 17-3 Two parallel plates are charged to produce a potential difference of 50 V. If the separation between the plates is 0.050 m, calculate the magnitude of the electric field in the space between the plates

E=1000 V/m

If the field is not uniform, it can be calculated at multiple points:

$$E_x = -\Delta V / \Delta x$$

Equipotential Lines



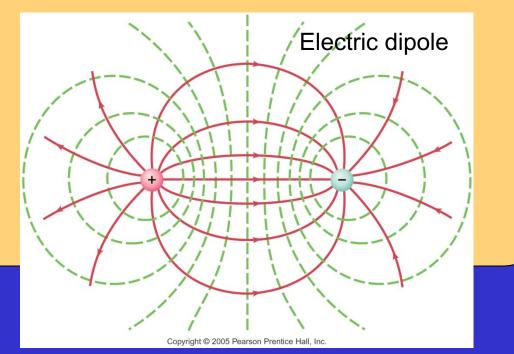
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Similar to topographic maps

An **equipotential** is a line or surface over which the **potential is constant**.

Electric field lines are **perpendicular** to equipotentials.

A conductor is entirely at the same potential in the static cases; the surface of a conductor is an equipotential.



Electric Potential

The **electric potential** due to a *point charge* can be derived using calculus.

$$E = k \frac{Q}{r^2}$$

$$V = k \frac{Q}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$$

$$V = k \frac{Q}{r} \text{ when } Q > 0$$

$$(a)$$

$$V = k \frac{Q}{r} \text{ when } Q > 0$$

$$(a)$$

$$V = k \frac{Q}{r} \text{ when } Q < 0$$

$$(b)$$

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NOTE: Joule is a very large unit for dealing with energies of electrons, atoms or molecules, this is why eV was introduced. One electron volt (eV) is the energy gained by an electron moving through a potential difference of one volt.

Exercises

 $W = -q(V_{\rm b} - V_{\rm a})$

$$V = k \frac{Q}{r}$$

Ex. 17-4 Determine the potential at a point 0.50 m (a) from a + 20μ C point charge, (b) from a - 20μ C point (a) $3.6 \times 10^5 V$ (b) $-3.6 \times 10^5 V$

Ex. 17-5 What minimum work must be done by an external force to bring a charge q = $3.00 \,\mu$ C from a great distance away (r: infinity) to a point 0.500 m from a charge Q = $20.0 \,\mu$ C ? 1.08 J

NOTE:

To find the electric field near a collection of two or more point charges requires adding VECTORS

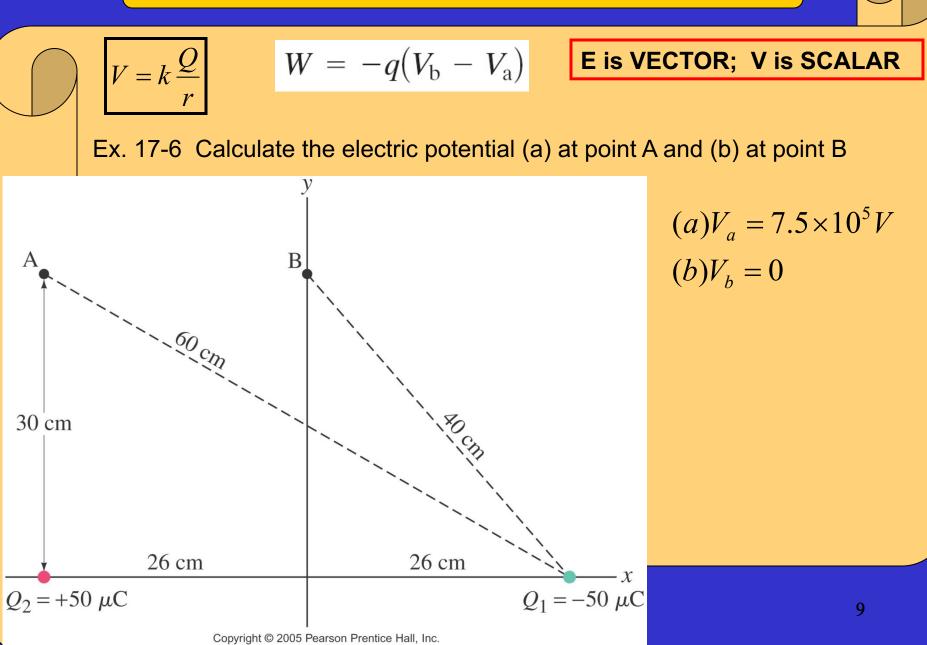
To find the electric potential near a collection of two or more point charges is EASIER, it only requires adding NUMBERS

NOTE:

Take the **sign** of the charge into account when calculating electric potential

E is VECTOR; V is SCALAR

Exercise



Electric Potential Energy of a System of Point Charges

 q_2

Potential ENERGY of q₂

 q_1

Potential created by
$$q_1$$
 at a distance r

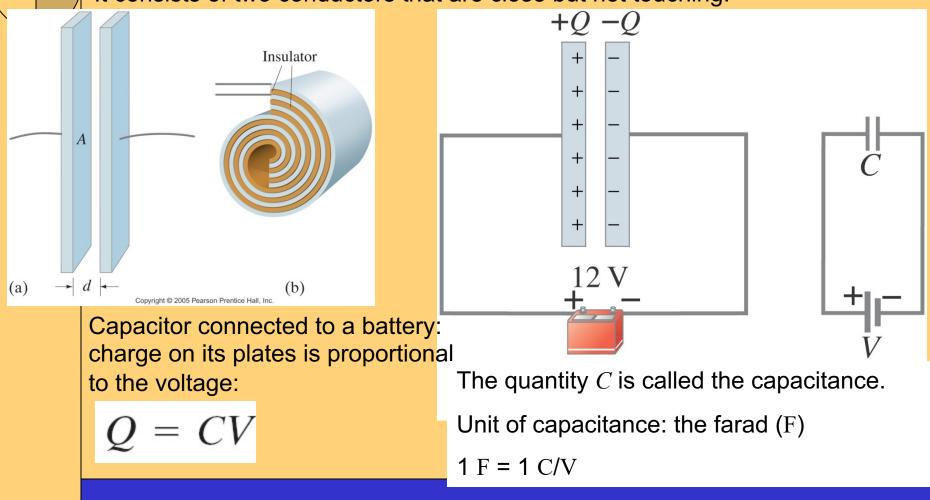
$$V = \frac{1}{4\pi\varepsilon_0} \frac{q_1}{r}$$

$$\mathsf{PE} = W = q_2 V = \frac{1}{4\pi\varepsilon_0} \frac{q_1 q_2}{r}$$

This is also the work done by an EXTERNAL force to bring q_2 from an infinity to a distance r from particle q_1

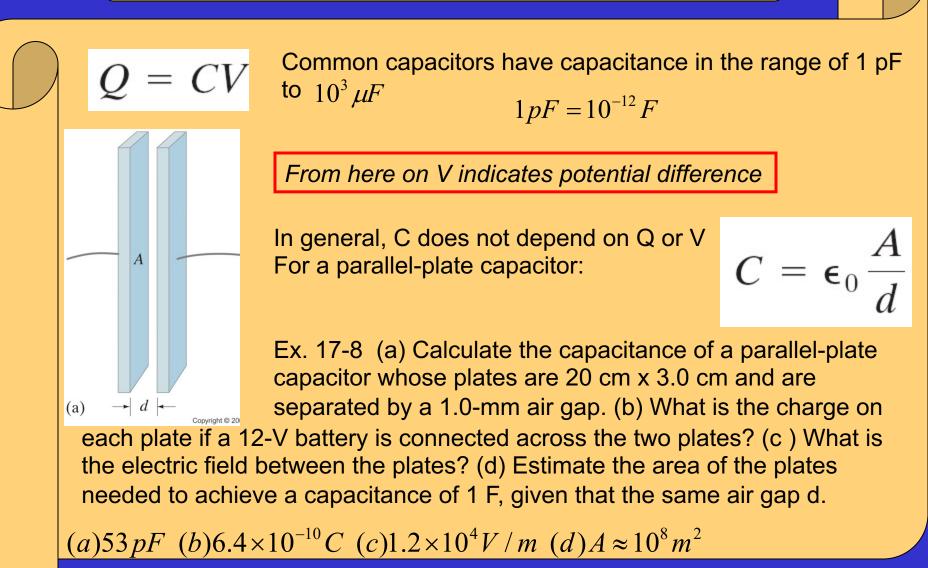
Capacitance

A capacitor is a device that can **store** electric charge. It consists of two conductors that are close but not touching.



Examples of capacitors: power backups, camera flash

Capacitance



$$\epsilon_0 = \frac{1}{4\pi k} = 8.85 \times 10^{-12} \,\mathrm{C}^2/\mathrm{N} \cdot \mathrm{m}^2$$
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Dielectrics

A dielectric is an insulator, and is characterized by a dielectric constant K.

Capacitance of a parallel-plate capacitor filled with dielectric:

Purpose of dielectrics:

 $C = K\epsilon_0 \frac{A}{d}$ (i) They do not break (control of 0 and 0 higher voltage can be applied (ii) Plates can be together without touching; C increases (iii) They increase C by K

Permittivity of the material $\mathcal{E} = K \mathcal{E}_0$

Ex. 17-9 An airfilled capacitor consisting of 2 parallel plates separated by a distance d is connected to a battery of voltage V and acquires a charge Q. While it is still connected to the battery, a slab of dielectric material with K=3 is inserted between the plates of the capacitor. Will Q increases, decrease, or stay the same? V stays constant, C increases, so Q increases as well

Ex. 17-10 Suppose the capacitor above is instead disconnected from the battery and then a dielectric is inserted between the plates. Will Q, C, or V change?

Q stays constant, C increases, so V decreases

A charged capacitor stores electric energy; the energy stored is equal to the work done to charge the capacitor.

$$\Delta W = V \Delta q \Rightarrow W = \frac{V_f}{2}Q \qquad \text{PE} = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C}$$

Ex. 17-11 A camera flash unit stores energy in a 150-mF capacitor at 200 V. How much electric energy can be stored?

PE=3.0J

For parallel plates
$$C = \epsilon_0 \frac{A}{d} \Rightarrow PE = \frac{1}{2}CV^2 = \frac{1}{2}\varepsilon_0 E^2 Ad$$

energy density $= \frac{PE}{volume} = \frac{1}{2}\epsilon_0 E^2$ This is true for any region, not just parallel

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plates